

Machine Learning In Model Based Engineering

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GLOBAL PRODUCT DATA INTEROPERABILITY **S U M M I T** 2018



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Presentation outline

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- **Model Based Engineering and Computational Design Synthesis (CDS)**
 - Design Synthesis done manually
 - CDS using Graph Transformations
- **Function Behavior Structure (FBS) role in CDS**
 - Framework for CDS
 - FBS Levels in Modeling
 - Role of Knowledge Based Engineering (KBE) in CDS
 - Building Functional Structures using MOKA (Methodology and software tools Oriented to Knowledge-based engineering Applications)
- **Behavior Modeling and Digital Twins**
 - Auto Suspension Systems, Production Systems
 - Need for Black Box modeling
 - Radial Basis Function Networks for Dynamic Black Box Modeling
 - Learning Dynamic Models
- **Proposed Workflow for CDS with Digital Twin**

Authors' bios

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- **Sunil Elanayar**

Joined Boeing in 2007 from Dassault Systemes. Currently an IT Manager in Engineering Systems. Managing teams working in MBSE, Product Standards. In the past, he has worked in Visualization, New Wiring Systems, Aerodynamics, Knowledge Based Engineering (KBE), Machine Learning, and Optimization.



- **Phillip Austin**

Boeing Software Developer with experience in BDS Engineering Systems, BDS Manufacturing Systems, IPDM Teamcenter, BCA Enovia. Currently working in BCA Product Standards and 2CES MBSE Development.



- **Juan Sanchez De Muniaín**

Software developer at Boeing since 2014, now on the 2CES PLM effort at Boeing; before that, developing computer-aided engineering and manufacturing applications primarily around product standards.

Enabling Model Based Engineering

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To Enable MBE capabilities, tools need the ability to:

- Model products at multiple levels of abstraction, i. e. Function, Behavior and Structure (FBS)
- Formalize Engineering Knowledge with a view to manipulate, transform, and reuse it.
- Enable the quick generation and adaptation of designs (especially in the conceptual phases.)
- Decrease the tedium in routine design tasks
- Support innovation in the design process
- Help keep behavioral models current in the light of IOT
- Support Computational Design Synthesis
- Support Digital Twin concepts

Benefits of Computational Design Synthesis (CDS):

1. Increases the efficiency of the design process and the creation of new solutions,
2. Facilitates design reuse during concept generation,
3. Enables the exploration of larger design solution spaces, and thereby removes psychological bias that may limit designers to previous solutions or to specific engineering domains.

The Process of Design Synthesis: Functional Decomposition

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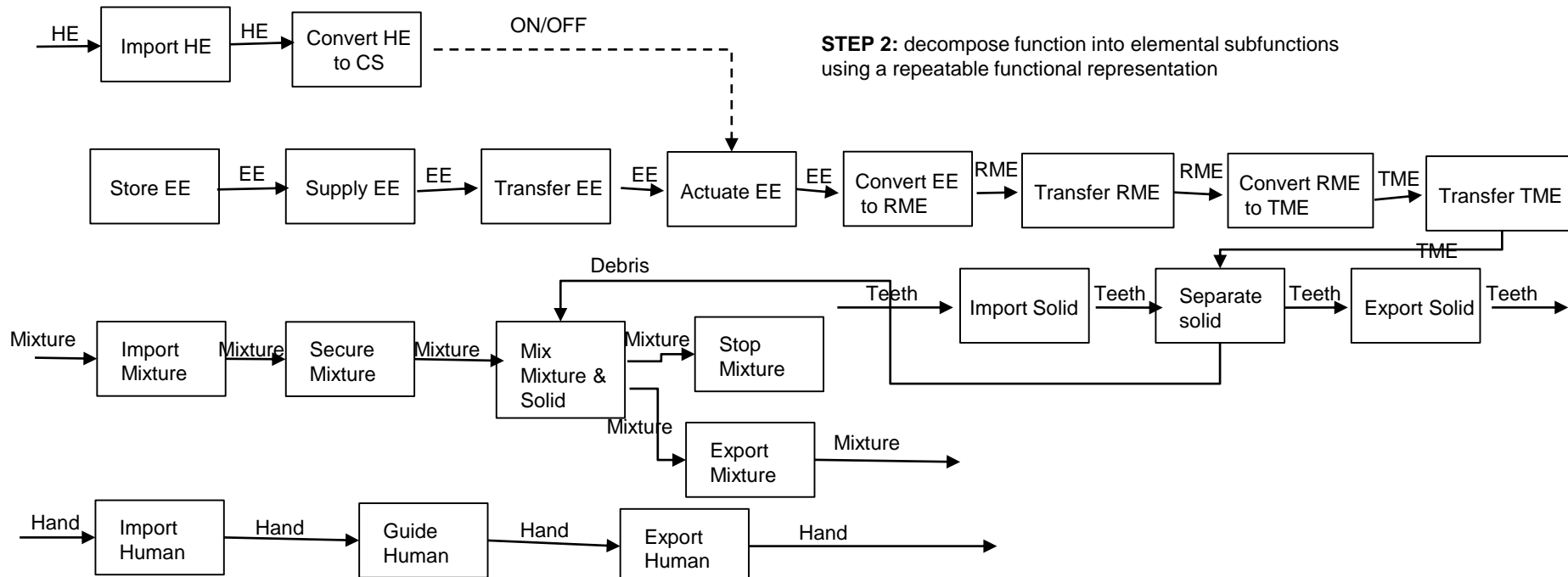
STEP1: transform customer needs into an overall product function



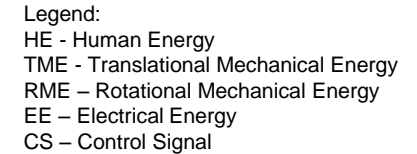
Legend:

HE - Human Energy
TME - Translational Mechanical Energy
RME - Rotational Mechanical Energy
EE - Electrical Energy
CS - Control Signal

STEP 2: decompose function into elemental subfunctions using a repeatable functional representation



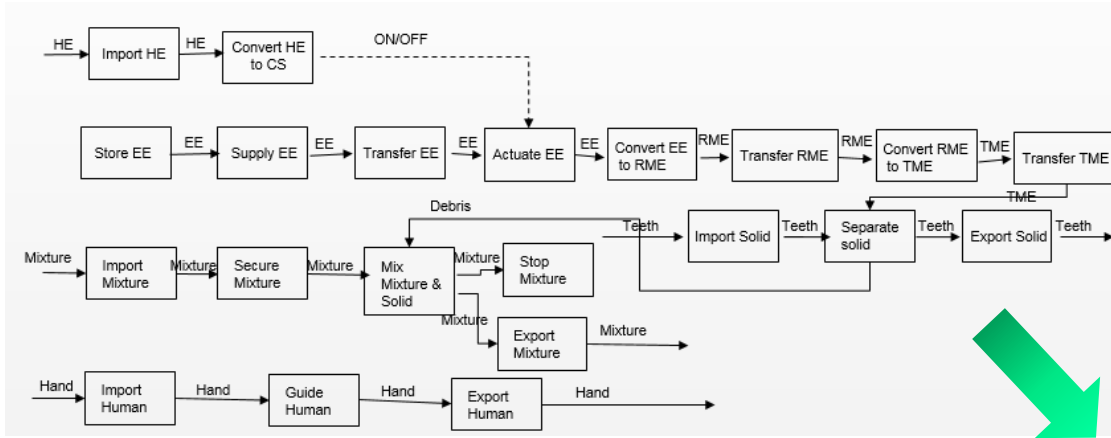
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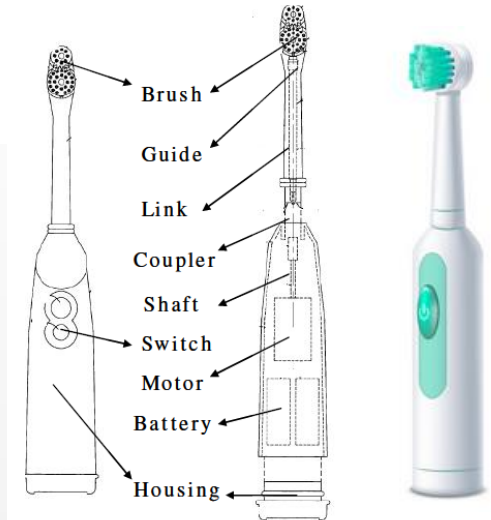
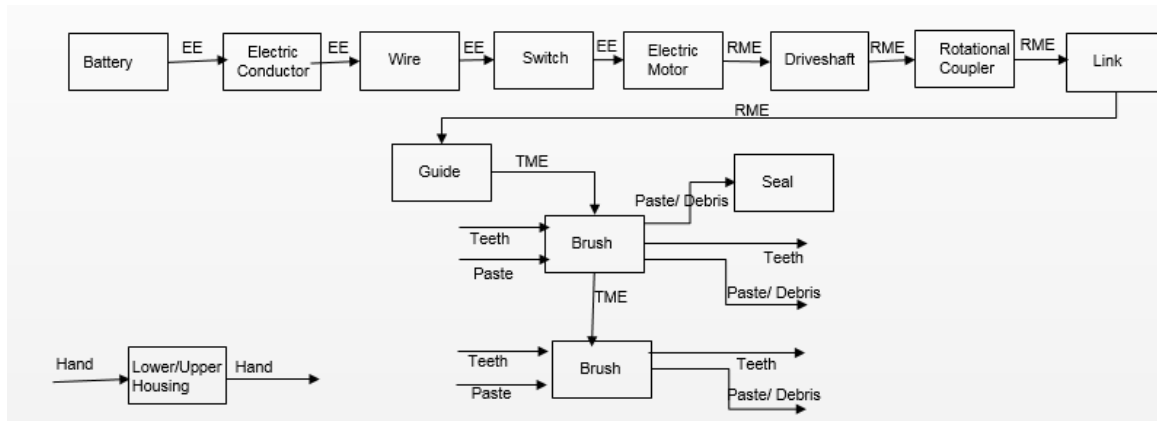
Computational Design Synthesis: Graph Transformations

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Function Structure of Electric Toothbrush

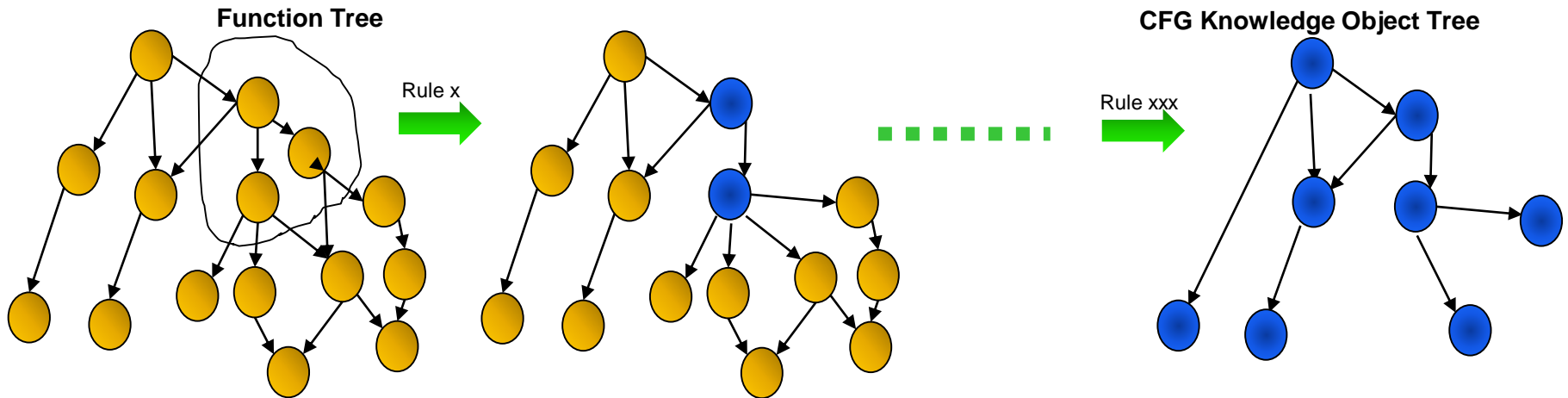
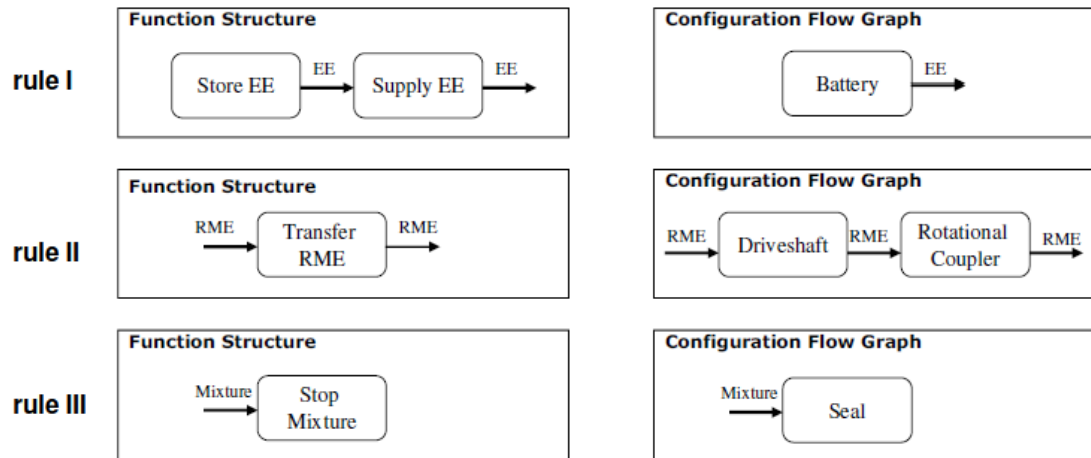


Configuration Flow Graph of Electric Toothbrush



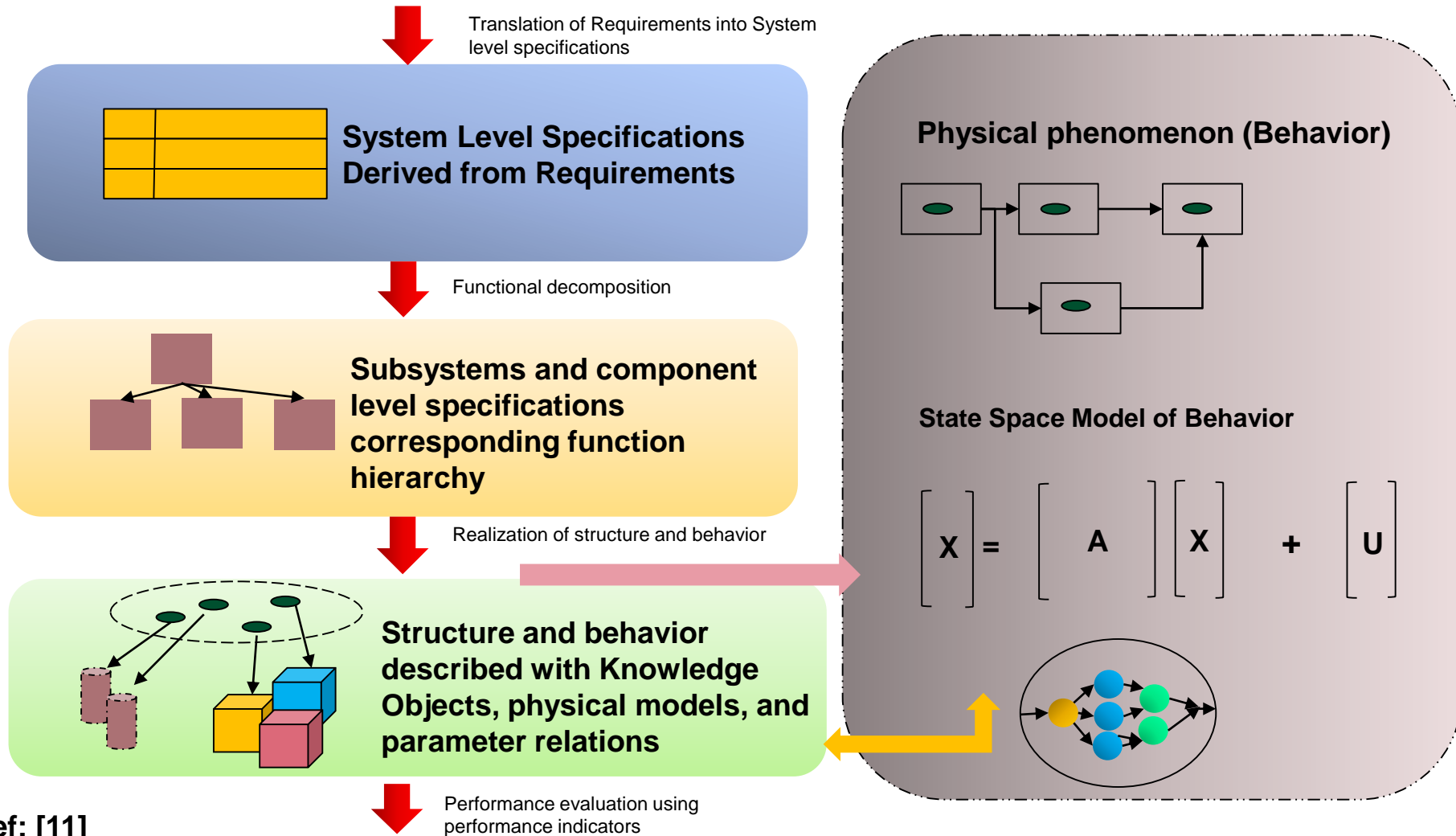
Graph Transformations / Graph Grammars

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FBS Framework for Computational Design Synthesis in MBE

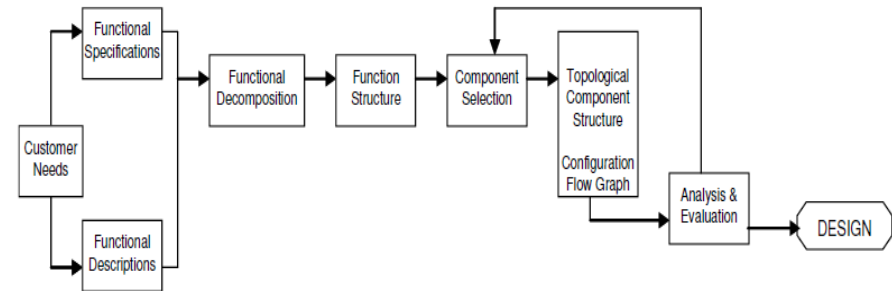
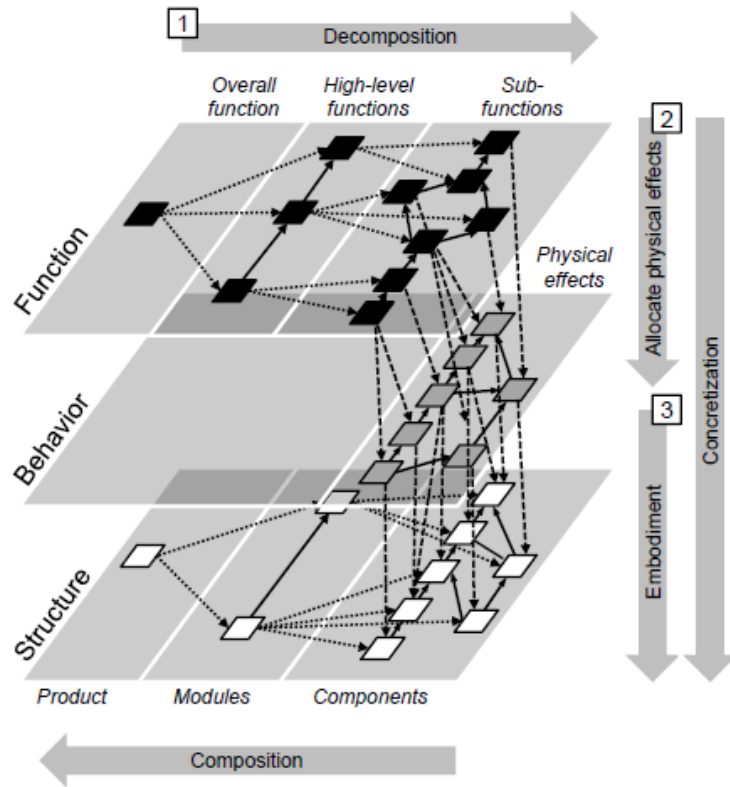
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Ref: [11]

FBS Levels and Process of Computational Design Synthesis

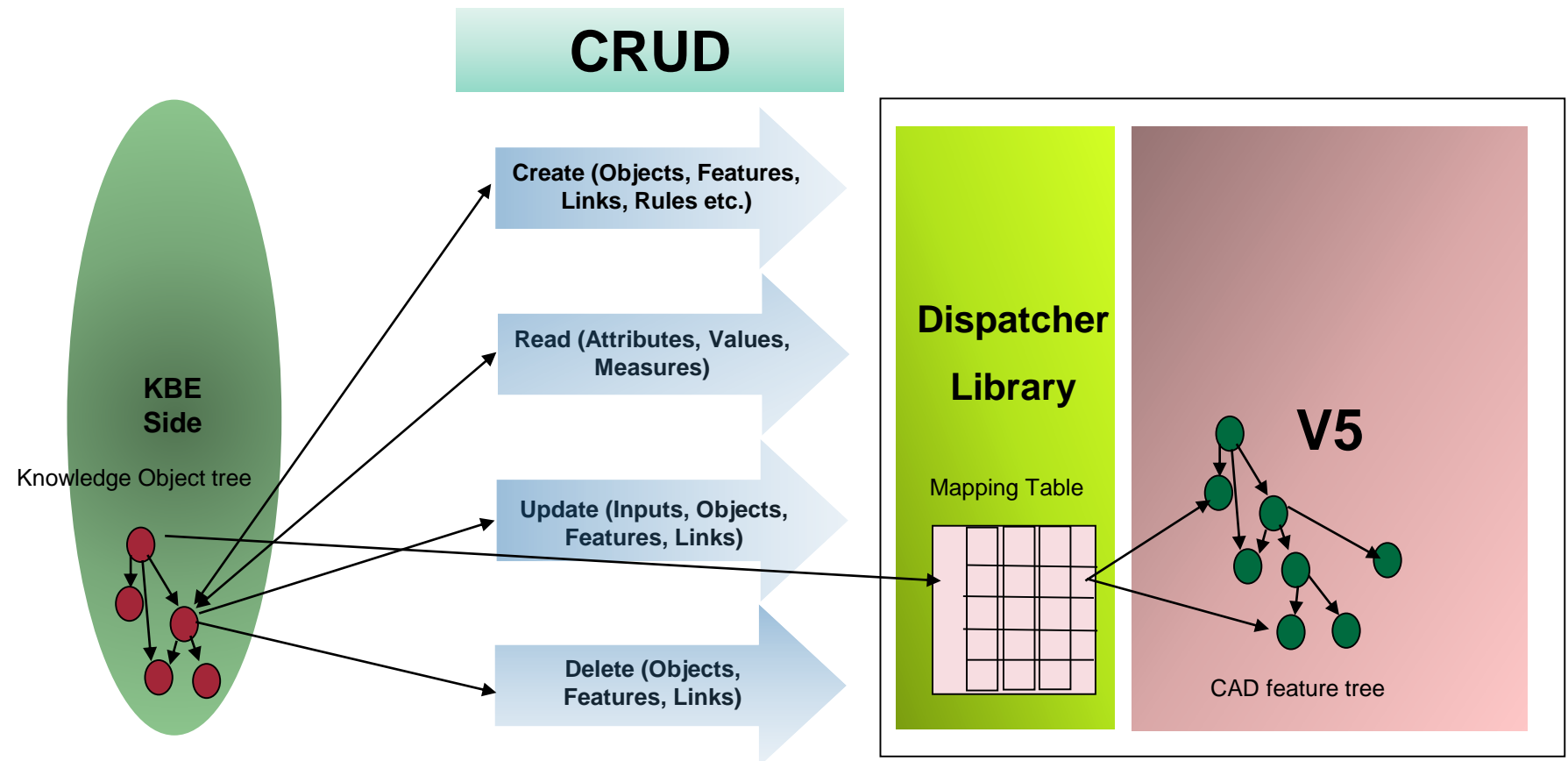
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Ref: [7,9]

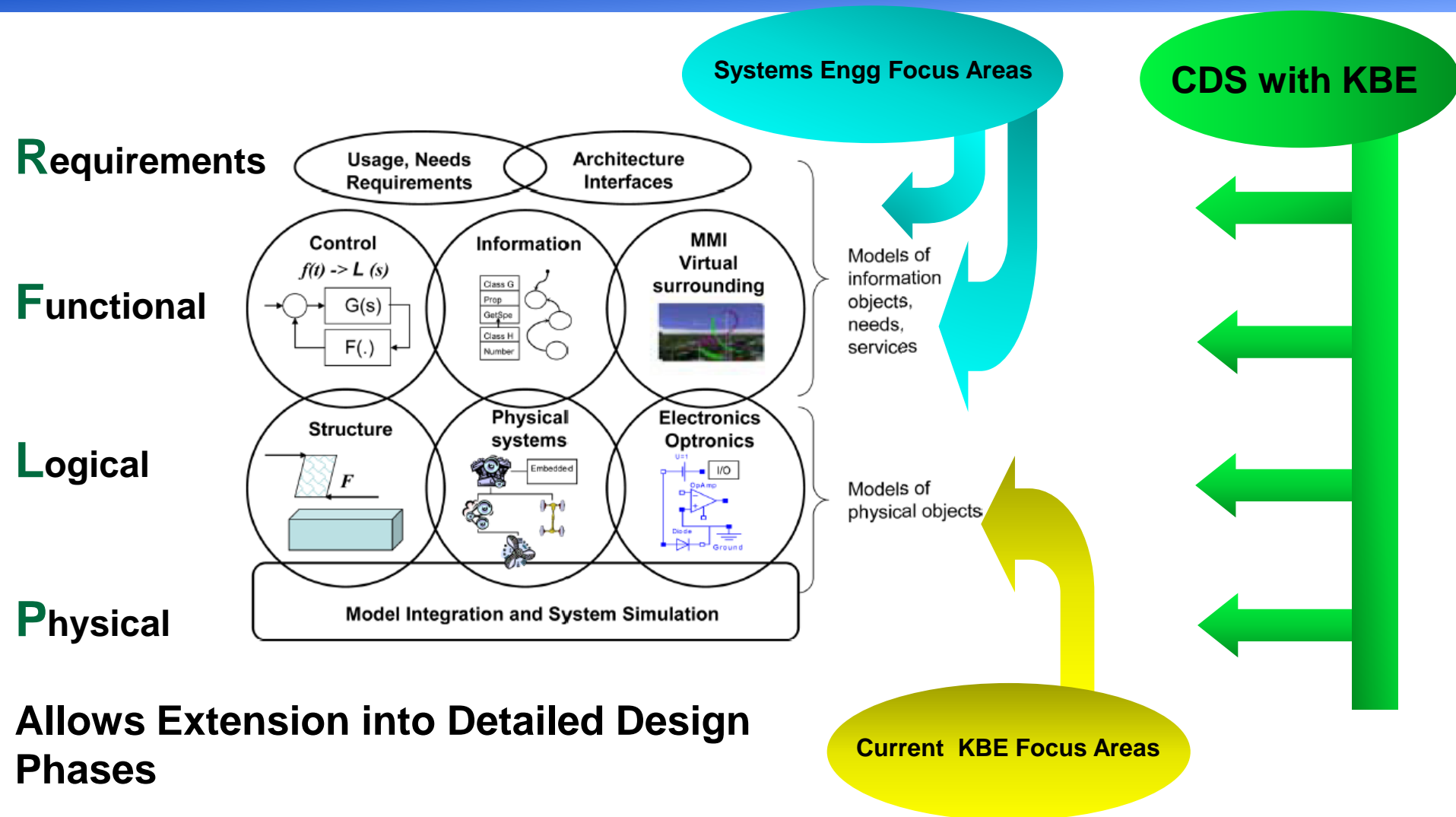
Knowledge Object Trees and CAD Interactions

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Enriching Computational Design Synthesis Using Knowledge Objects

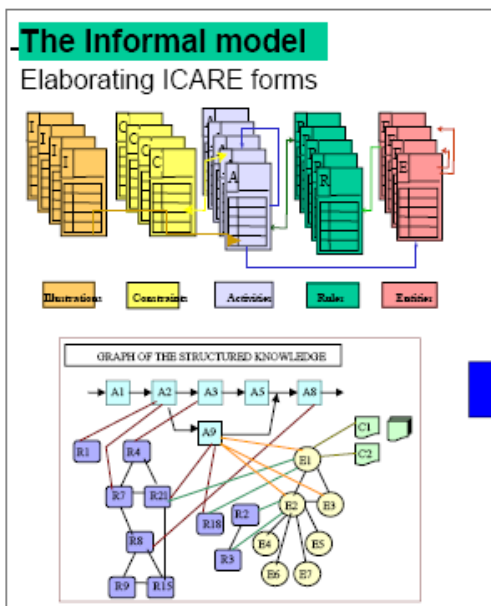
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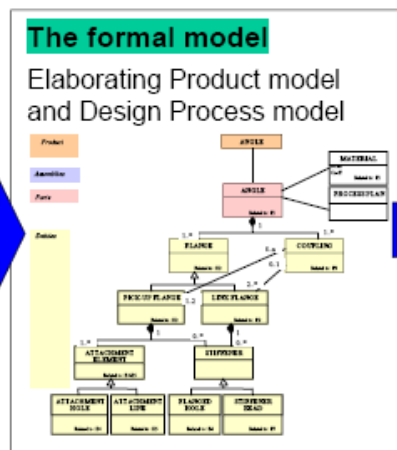
Using MOKA ICARE forms to build Functional Structure Graphs

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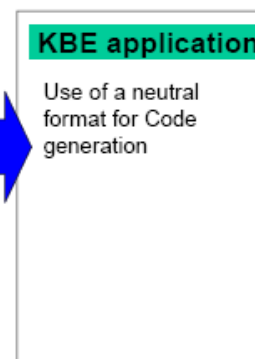
Functional
Structure



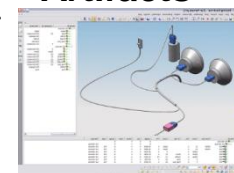
Knowledge
Configuration
Flow Graph



Instantiate
with Input
Parameters



CAD/PDM
Artifacts



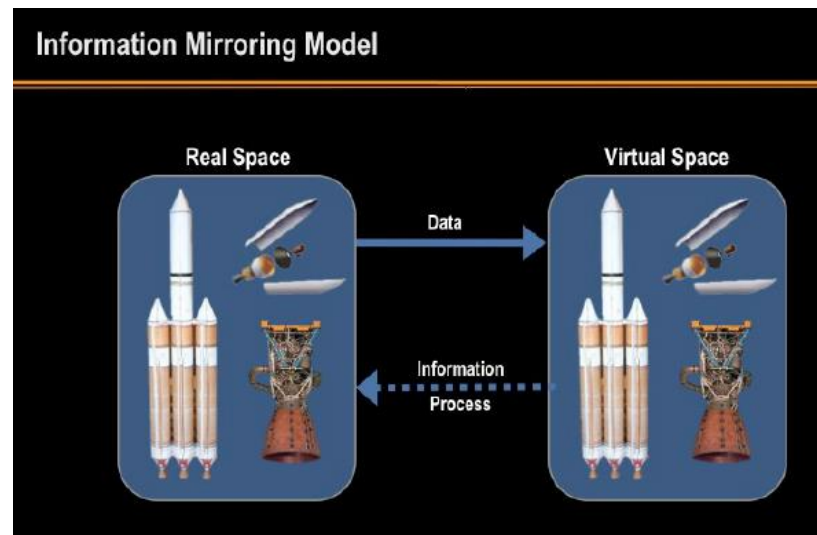
- ICARE forms are templates that store the knowledge in five categories:
 - Illustrations– for describing any case studies or relevant examples
 - Constraints– limitations on Entities
 - Activities– the description of the elements of the design process
 - Rules– the means of regulating the Activities and providing the ‘know-how’ or strategy of the design process
 - Entities– the objects that describe the product (Entities may be further classified into E-structure and E-function)

Digital Twins: What are they good for?

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Digital twins help manufacturers and OEMs by helping with:

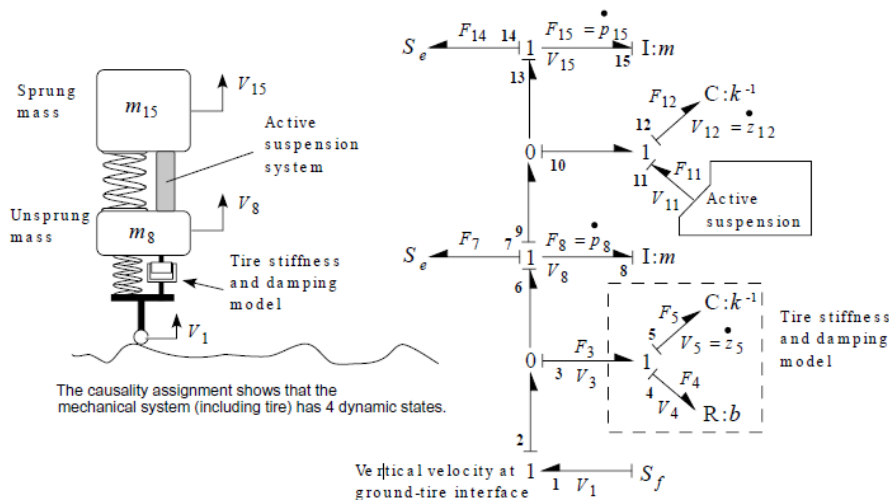
- Visualizing products in use, by real users, in real-time
- Building a digital thread, connecting disparate systems and promoting traceability
- Refining assumptions with predictive analytics
- Troubleshooting far away equipment
- Managing complexities and linkage within systems-of-systems
- Shared Conceptualization, Comparison, and Collaboration



Ref: [16]

Behavior Modeling and The Digital Twin

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State Space Equations

$$\dot{Z} = AZ + BF_a + \dot{Z}_r$$

$$\begin{bmatrix} \dot{Z}_1 \\ \dot{Z}_2 \\ \dot{Z}_3 \\ \dot{Z}_4 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & -1 \\ -K_s/M_{us} & -C_s/M_{us} & 0 & C_s/M_{us} \\ 0 & 0 & 0 & 1 \\ -K_s/M_s & C_s/M_s & -K_{us}/M_s & -C_s/M_s \end{bmatrix} \begin{bmatrix} Z_1 \\ Z_2 \\ Z_3 \\ Z_4 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ -1 \\ 0 \end{bmatrix} \dot{Z}_r$$

Ref: [4]

$$M_s \ddot{Z}_s + C_s(\dot{Z}_s - \dot{Z}_{us}) + K_s(Z_s - Z_{us}) = 0 \quad (1)$$

$$M_{us} \ddot{Z}_{us} + C_s(\dot{Z}_{us} - \dot{Z}_s) + K_s(Z_{us} - Z_s) + K_{us}(Z_{us} - Z_r) = 0 \quad (2)$$

$$\ddot{Z}_s = \frac{1}{M_s} [C_s(\dot{Z}_{us} - \dot{Z}_s) + K_s(Z_{us} - Z_s)] \quad (3)$$

$$\ddot{Z}_{us} = \frac{1}{M_{us}} [C_s(\dot{Z}_s - \dot{Z}_{us}) + K_s(Z_s - Z_{us}) + K_{us}(Z_r - Z_{us})] \quad (4)$$

Let us assume the state variables are

$$Z_1 = Z_s - Z_w$$

$$Z_2 = \dot{Z}_s$$

$$Z_3 = Z_w - Z_r$$

$$Z_4 = \dot{Z}_w$$

$$\dot{Z}_1 = \dot{Z}_s - \dot{Z}_w \approx Z_s - Z_w$$

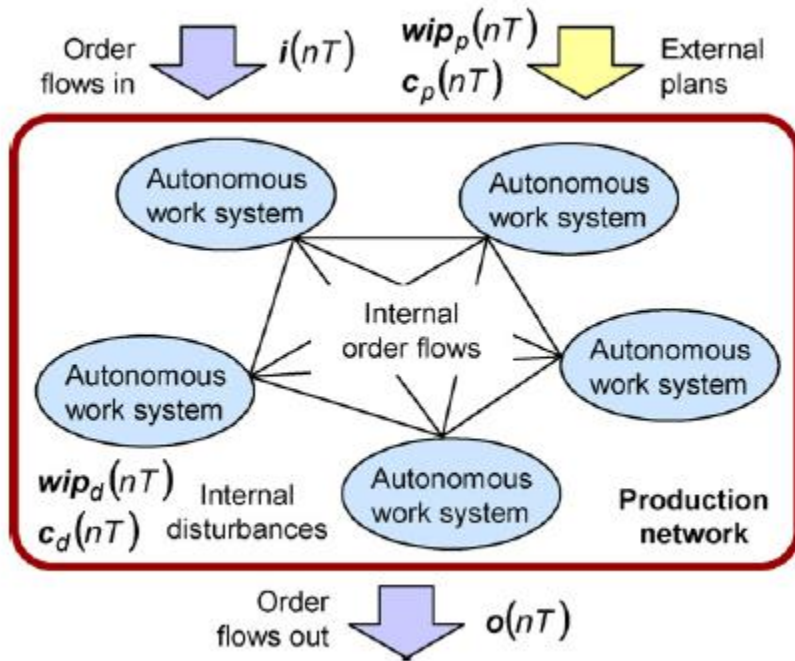
$$\dot{Z}_2 = \ddot{Z}_s$$

$$\dot{Z}_3 = \dot{Z}_w - \dot{Z}_r \approx Z_4 - \dot{Z}_r$$

$$\dot{Z}_4 = \ddot{Z}_w$$

Modeling Production Systems for Digital Twin

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$$\begin{bmatrix} z\mathbf{w}_i(z) \\ z\mathbf{w}_o(z) \\ z^d\mathbf{c}_m(z) \end{bmatrix} = \begin{bmatrix} \mathbf{I} & \mathbf{0} & TP^T \\ \mathbf{0} & \mathbf{I} & TI \\ k_c\mathbf{I} & -k_c\mathbf{I} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{w}_i(z) \\ \mathbf{w}_o(z) \\ \mathbf{c}_m(z) \end{bmatrix} + \begin{bmatrix} TI & \mathbf{0} & \mathbf{0} & TP^T & -TP^T \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & TI & -TI \\ \mathbf{0} & k_c\mathbf{I} & -k_c\mathbf{I} & \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{i}(z) \\ \mathbf{w}_d(z) \\ wip_p(z) \\ \mathbf{c}_p(z) \\ \mathbf{c}_d(z) \end{bmatrix}$$

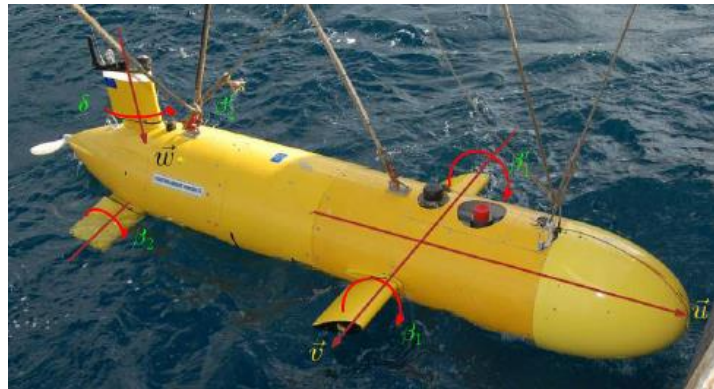
$$\begin{bmatrix} \mathbf{w}_i(z) \\ \mathbf{w}_o(z) \\ \mathbf{c}_a(z) \\ wip_a(z) \end{bmatrix} = \begin{bmatrix} \mathbf{I} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{I} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{I} \\ \mathbf{I} & -\mathbf{I} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{w}_i(z) \\ \mathbf{w}_o(z) \\ \mathbf{c}_m(z) \end{bmatrix} + \begin{bmatrix} \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{I} & -\mathbf{I} \\ \mathbf{0} & \mathbf{I} & \mathbf{0} & \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{i}(z) \\ \mathbf{w}_d(z) \\ wip_p(z) \\ \mathbf{c}_p(z) \\ \mathbf{c}_d(z) \end{bmatrix}$$

State Space Equations

Ref: [6]

Underwater Autonomous Vehicle Dynamics

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Axial propeller to control the velocity in Ox direction and 5 independent mobile fins :

- 2 horizontal fins in the front part of the vehicle (b1, b01).
- 1 vertical fin at the tail of the vehicle (d).
- 2 fins at the tail of the vehicle (b2, b02).

State Space Equations

Ref: [17]

Physical model:

$$M\dot{v} = G(v)v + D(v)v + \Gamma_g + \Gamma_u$$

$$\dot{\eta} = J_c(\eta_2)v$$

where:

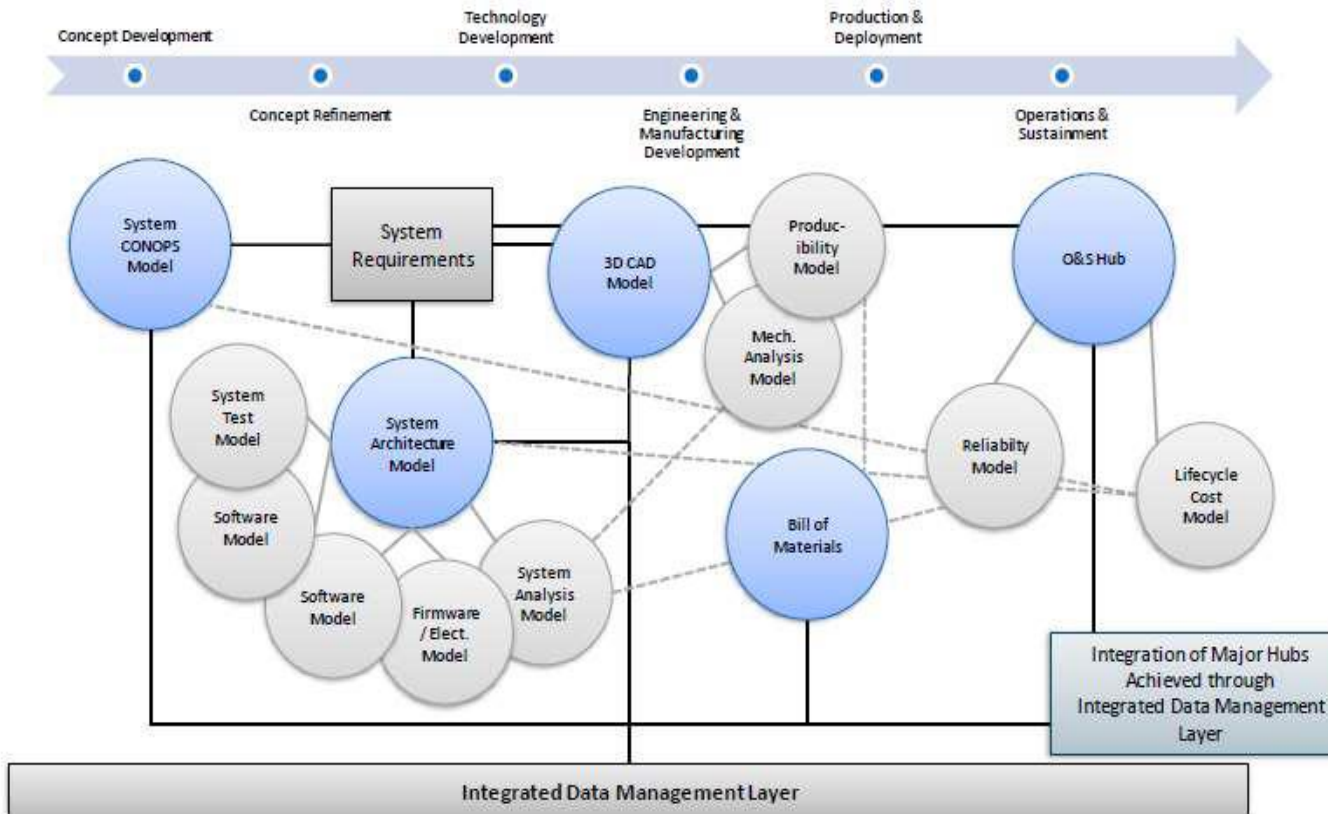
- M : mass matrix: real mass of the vehicle augmented by the "water-added-mass" part,
- $G(v)$: action of Coriolis and centrifugal forces,
- $D(v)$: matrix of hydrodynamics damping coefficients,
- Γ_g : gravity effort and hydrostatic forces,
- $J_c(\eta_2)$: referential transform matrix,
- Γ_u : forces and moments due to the vehicle's actuators.

A 12 dimensional state vector : $X = [\eta(6) \quad v(6)]^T$.

- $\eta(6)$: position in the inertial referential: $\eta = [\eta_1 \quad \eta_2]^T$ with $\eta_1 = [x \quad y \quad z]^T$ and $\eta_2 = [\phi \quad \theta \quad \psi]^T$. x , y and z are the positions of the vehicle , and ϕ , θ and ψ are respectively the roll, pitch and yaw angles.
- $v(6)$: velocity vector, in the local referential (linked to the vehicle) describing the linear and angular velocities (first derivative of the position, considering the referential transform: $v = [v_1 \quad v_2]^T$ with $v_1 = [u \quad v \quad w]^T$ and $v_2 = [p \quad q \quad r]^T$

Need for Low fidelity Behavioral Models for Digital Twins

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Models needed everywhere, but,

- What if you don't have one from first principles?
- Are they the right fidelity?
- How do you address all disciplines?
- How do you keep them up to date?
- What about the data deluge with IOT?
- Is learning and adaptation built into the models over its lifecycle?
- Do the models apply uniformly to different levels of abstraction?

Ref: [1]

Generic Dynamic Models

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Black Box Model

Feedback /
Learning

$$\begin{aligned}x_{k+1} &= f(x_k, u_k) + w_k \\ y_k &= h(x_k) + v_k \text{ for } k = 0, 1, 2, \dots\end{aligned}$$

State Equations

Sensor 1

Sensor 4

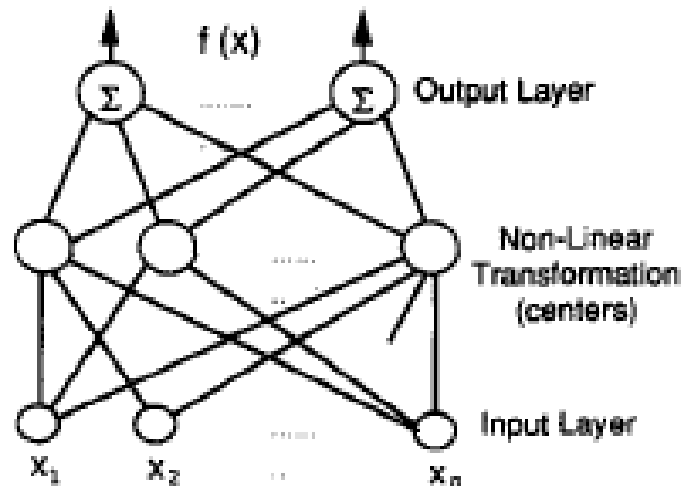
Sensor 2

Sensor 3

Black Box Neural Networks Models

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Radial Basis Function Networks



$$t_p(X) = \sum_{j=1}^p \lambda_j^p \Phi(\|X - X_j^c\|) + \lambda_0^T X$$

$$|t_p(X) - F(X)| \rightarrow 0$$

$$\Phi(r) =$$

$$r^2 \log r$$

Duchon

$$\sqrt{c + r^2}$$

Hardy

$$r^l \text{ (} l \text{ an odd integer)}$$

Thin Plate

$$\exp(-r^2)$$

Schagen

$$x_{k+1}^i = [\Lambda \quad \Lambda_0] \begin{bmatrix} \Psi(X_k^i) \\ X_k^i \end{bmatrix} + w_k^i$$

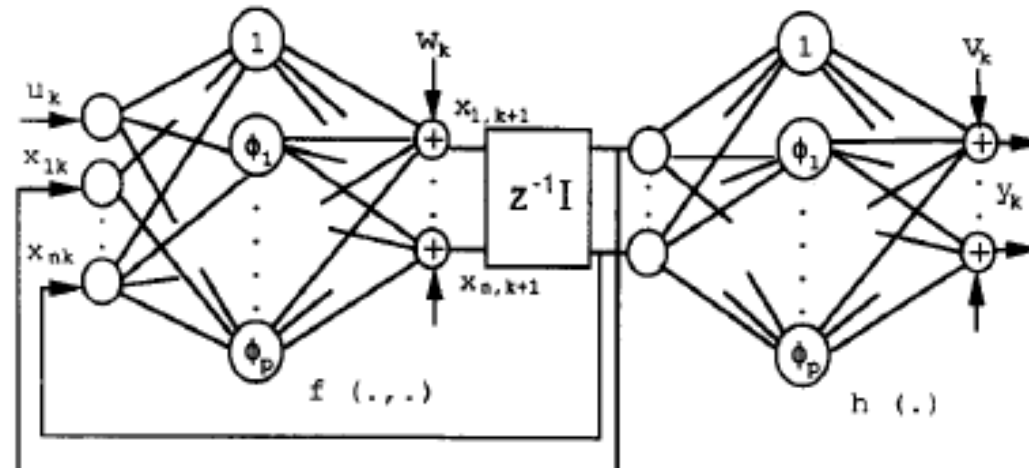
$$z_k^i = x_k^i + \zeta_k^i$$

Ref: [5]

Approximate System Equations

Training the Network

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Training / System Identification

$$\hat{\Theta}_{N+1} = \hat{\Theta}_N + R_N \hat{\xi}_{N-1}^T \left[I + \hat{\xi}_N R_N \hat{\xi}_{N-1}^T \right]^{-1} \times \left[\gamma_{N+1} - \hat{\xi}_N \hat{\Theta}_N \right]$$

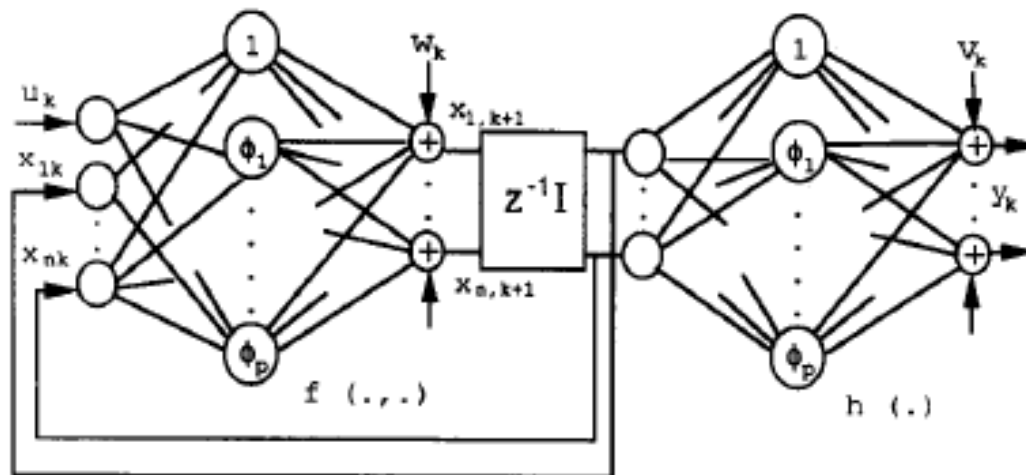
$$R_{N+1} = R_N - R_N \hat{\xi}_{N-1}^T \left[I + \hat{\xi}_N R_N \hat{\xi}_{N-1}^T \right]^{-1} \hat{\xi}_N R_N$$

Ref: [5]

Using the Learned system

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State Estimation Using Learned System



$$\hat{x}(k+1) = f'(\hat{x}_k, u_k) + F\hat{x}_k + bu_k + K_k[y_k - h'(\hat{x}_k) - H\hat{x}_k]$$

$$K_k^* = (2 + e_f)F\hat{P}_kH^T \left[(2 + e_f)H\hat{P}_kH^T + V \right]^{-1}$$

$$\begin{aligned} \hat{P}_{k+1} = & l_1(F - K_kH)\hat{P}_k(F - K_kH)^T + l_2I + l_3Tr(\hat{P}_k)I \\ & + l_4K_kK_k^T + l_5Tr(\hat{P}_k)K_kK_k^T + W + K_kVK_k^T \end{aligned}$$

$$\hat{P}_0 = \rho_0.$$

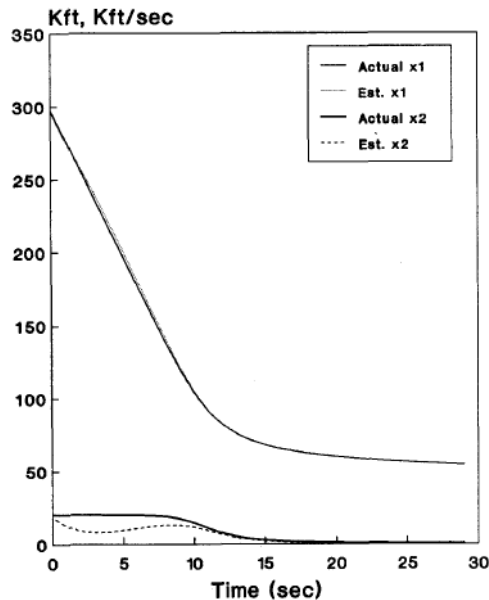
Ref: [5]

Viability of Learned Network for Modeling Dynamic Systems

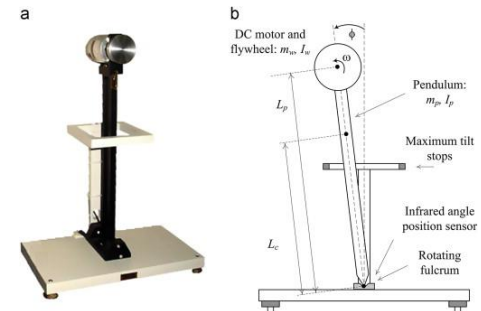
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$$\begin{bmatrix} x_{1,k+1} \\ x_{2,k+1} \end{bmatrix} = \begin{bmatrix} x_{1k} - Tx_{2k} \\ x_{2k} - 3Tx_{2k}^2 e^{-0.05x_{1k}} \end{bmatrix}$$

$$y_k = \sqrt{10000 + x_{1k}^2} + \nu_k$$

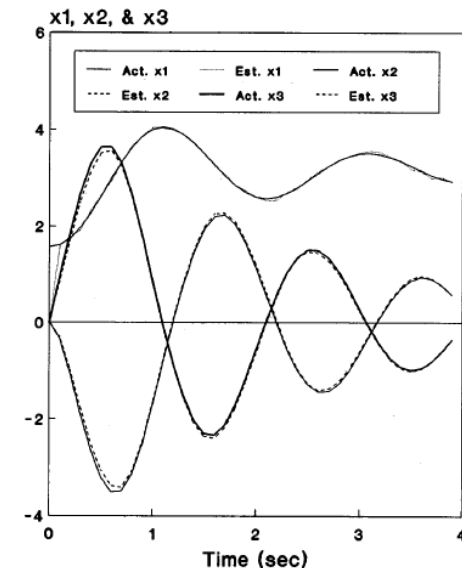


$$\begin{bmatrix} x_{1,k+1} \\ x_{2,k+1} \\ x_{3,k+1} \end{bmatrix} = \begin{bmatrix} x_{1k} + Tx_{2k} \\ x_{2k} + T(9.8 \sin x_{1k} + x_{3k}) \\ x_{3k} - 10T(x_{2k} + x_{3k}) \end{bmatrix}$$



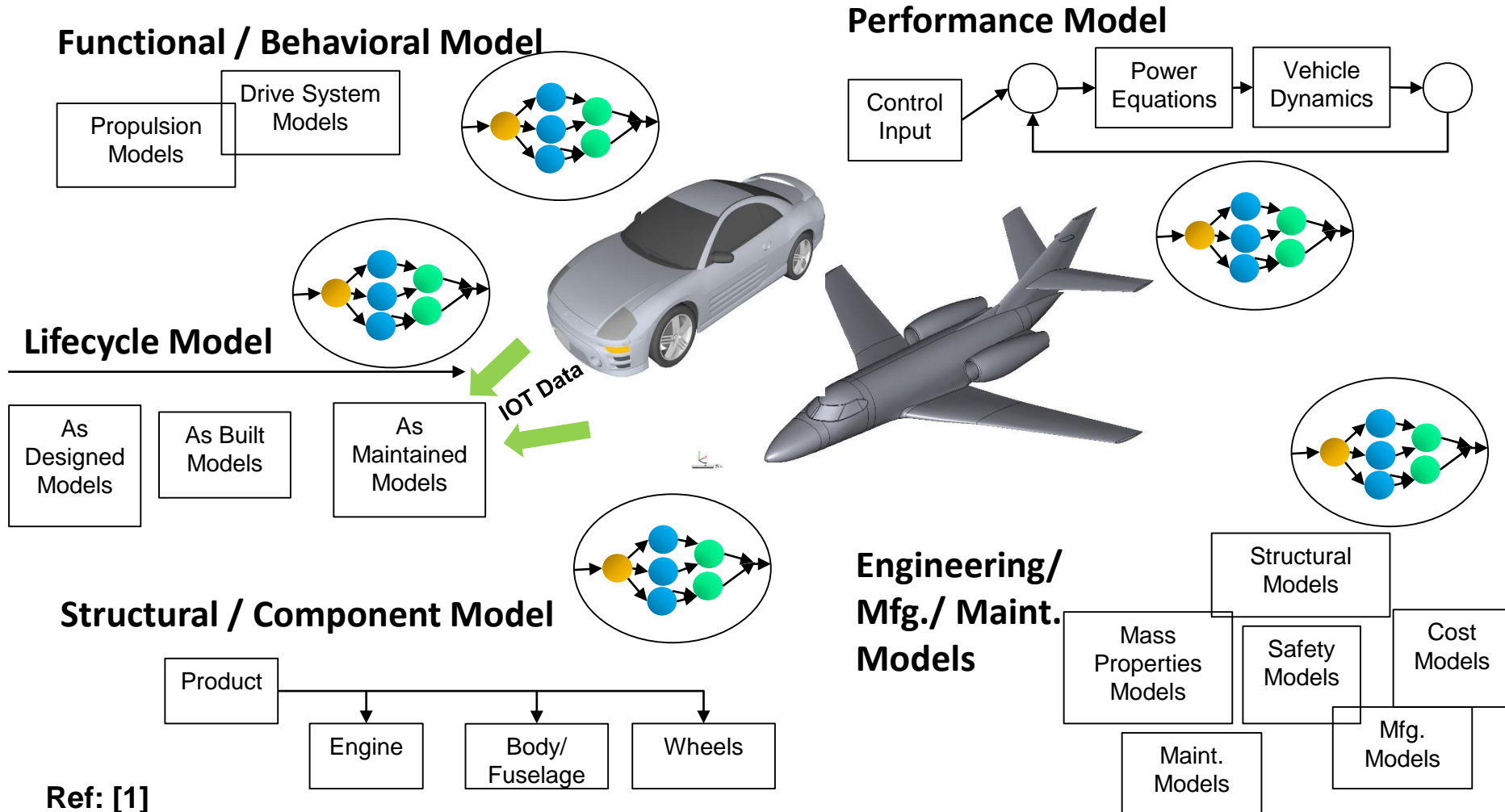
Inverted Pendulum

Ref: [5]



Learning Dynamic Black Box models

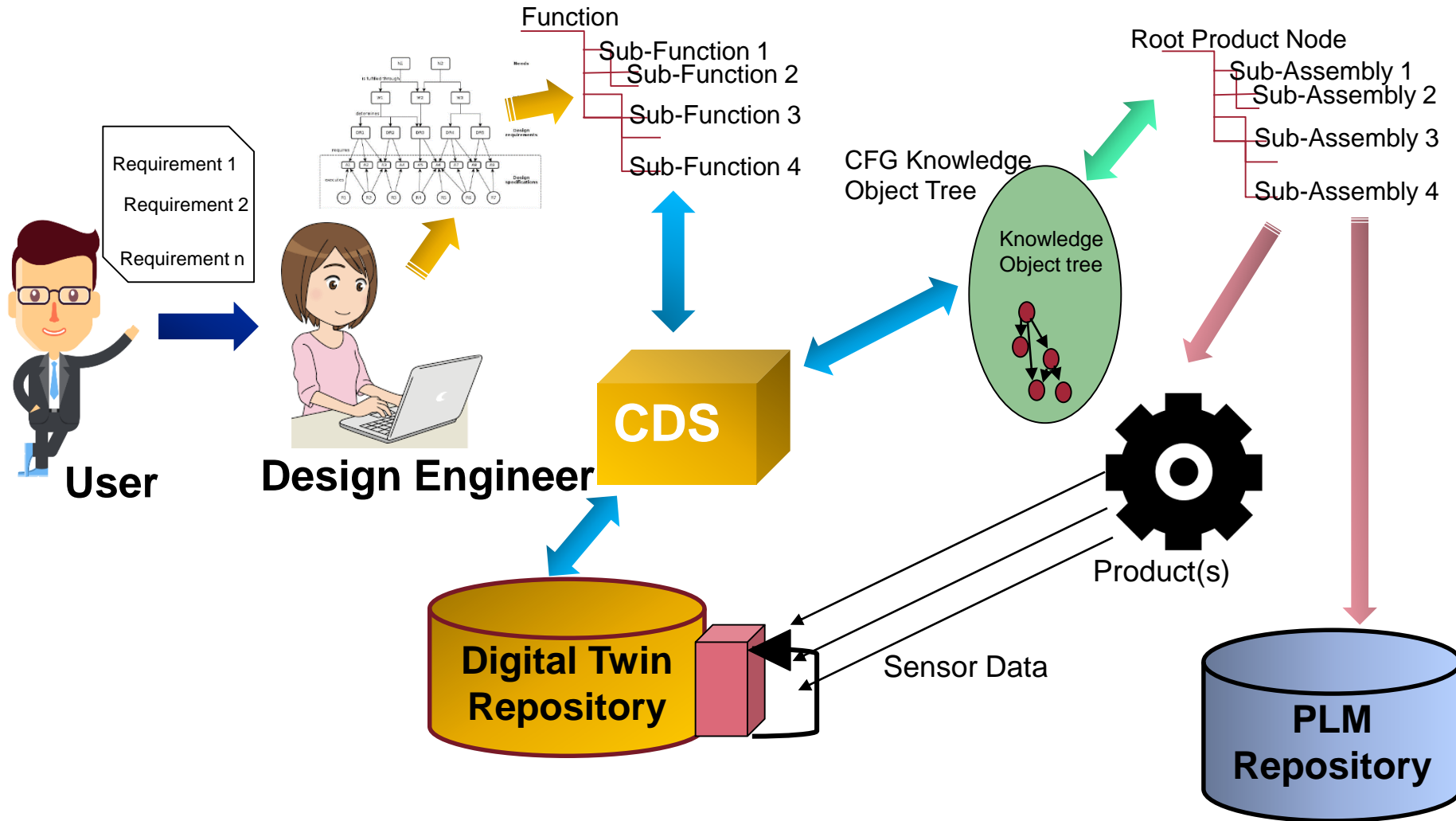
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Ref: [1]

Proposed Workflow for CDS with Digital Twin

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Questions?

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